

所別：通訊工程學系碩士班 甲組(一般生) 科目：通訊系統

1. [16 pts.] Referring to Figure 1, an input $n(t)$ to a filter with impulse response $h_1(t) = \text{sinc } 2Wt = \frac{\sin 2\pi Wt}{2\pi Wt}$ is a nonbandlimited white Gaussian process with $E\{n(t)\} = 0$ and $E\{|n(t)|^2\} = \sigma^2$, where $E\{\}$ is the expectation operation.

- Find the mean of the output $x(t)$. [3 pts.]
- Calculate the autocorrelation function of the output $x(t)$. [4 pts.]
- Find the joint probability density function of the output $x(t)$ at the time instants t_1 and t_2 . [4 pts.]
- If the spectral density of $y(t)$ is $S_y(f) = \begin{cases} \alpha^2, & |f| < B \\ 0, & \text{otherwise} \end{cases}$ and $B < W$, please find the transfer function of the filter $h_2(t)$. [5 pts.]

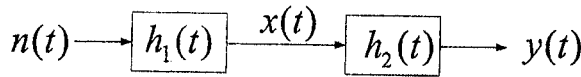


Figure 1.

2. [16 pts.] The following Figure 2 is a single sideband (SSB) system,

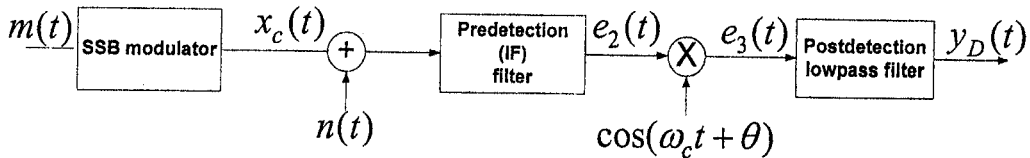


Figure 2.

where $m(t)$ is the baseband message signal with a bandwidth W and average power P , and $n(t)$ is an additive white Gaussian noise with double-sided power spectral density $N_0/2$.

- If lower-sideband SSB is employed, please describe how you generate the lower-sideband SSB signal $x_c(t)$. [4 pt.]
 - What is the minimum required bandwidth of the predetection bandpass filter? [3 pts.]
 - Find the predetection SNR (measured at the output of the predetection IF filter). [4 pts.]
 - Find the postdetection SNR (measured at the output of the postdetection lowpass filter). [5 pts.]
3. [18 pts.] Please judge whether the statement is true or false and explain for your answer.
- No matter how close together we sample a bandlimited white Gaussian noise process, samples are independent. [6 pts.]
 - If a random process with sample function $n(t) = A \cos(\omega_0 t + \varphi)$ where A and ω_0 is a constant and φ is a random variable with pdf $f(\varphi) = \begin{cases} 1/\pi, & |\varphi| \leq \pi/2 \\ 0, & \text{otherwise} \end{cases}$, then the process $n(t)$ is not an ergodic process. [6 pts.]
 - Consider the analog signal $x_a(t) = 3 \cos(2000\pi t) + 5 \sin(6000\pi t) + 10 \cos(12000\pi t)$. If we sample this signal using a sampling rate $f_s = 8 \text{ kHz}$ and $x(nT_s)$ is the sampled signal with $T_s = 1/f_s$, then we can reconstruct the signal $x_a(t)$ by using the ideal interpolation as $\frac{2B}{f_s} \sum_{n=-\infty}^{\infty} x(nT_s) \text{sinc}\{2B(t - nT_s)\}$ if $B > f_s$. [6 pts.]

注意：背面有試題

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4. [20 pts.] Consider BPSK in symbol interval $[0, T]$. The signals $A \cos \omega_c t$ and $-A \cos \omega_c t$ are transmitted for the information bit $b=1$ and $b=0$, respectively. Assume the channel is the AWGN channel with double-sided power spectral density $N_0/2$. At the receiver, the matched filter with impulse response $h(t) = k \Pi((t-T/2)/T) \cos(2\pi f_c t)$ is used $\Pi(t) = \begin{cases} 1, & |t| < 1/2 \\ 0, & \text{otherwise} \end{cases}$. Let E_b denote the energy per bit and $v(t)$ denote the output signal of the matched filter. The value of k is chosen such that $v(t)$ is equal to $1+N$ or $-1+N$, where N is a zero-mean random variable. The detected value of b at the receiver is denoted by \hat{b} .
- (a) Find the variance of N . [6 pts.]
- (b) Determine the channel capacity (bits/symbol) if $\hat{b} = \begin{cases} 1, & v(T) > 0 \\ 0, & \text{otherwise} \end{cases}$. [7 pts.]
- (c) Determine the channel capacity (bits/symbol) for the following decision rule. If $-0.5 \leq v(T) \leq 0.5$, the received information is discarded; otherwise, $\hat{b} = \begin{cases} 1, & v(T) > 0.5 \\ 0, & v(T) < -0.5 \end{cases}$. Assume that E_b/N_0 is large enough such that the probability of $N \geq 1.5$ is almost equal to zero. [7 pts.]
5. [12 pts.] Consider 16-QAM with signal sets of the form $s_i(t) = a_i \cos \omega_c t + b_i \sin \omega_c t$, where $a_i, b_i \in \{\pm A, \pm 3A\}$.
- (a) For transmission rate 4 bits/ T , 16 signals in one symbol interval $[0, T]$ are used with equal probability. Find the average energy **per bit**. [4 pts.]
- (b) For transmission rate 3 bits/ T , there are two choices: (1) choose 8 signals with the lowest average energy from 16-QAM in one symbol interval $[0, T]$ (or $[T, 2T]$). (2) choose 64 two-symbol signals with the lowest average energy (each two-symbol signal consists of one signal in $[0, T]$ and one signal in $[T, 2T]$) from all possible 256 two-symbol signals. To minimize average energy per bit, which one is preferred? Also find the minimum value of the average energy **per bit**. [8 pts.]
6. [18 pts.] Consider the modulation scheme with signals given as
- $$s_i(t) = A_i \cos(\omega_c t + B_i), \quad 0 \leq t \leq T, \quad i=1, 2, \dots, 8$$
- where $B_i = \frac{\pi}{4}(i-1)$ and $A_i = \begin{cases} r_1, & i \text{ is odd} \\ r_2, & i \text{ is even} \end{cases}$ ($r_1 \leq r_2$). Note that when $r_1 = r_2$, this modulation is 8PSK.
- (a) Devise an optimal coherent detector, which minimizes the symbol error probability, and show the optimal decision region. [10 pts.]
- (b) Determine the value of $\frac{r_2}{r_1}$ such that the symbol error probability can be minimized for a given average energy. [8 pts.]