Find orthogonal trajectories of the following function

$$y = c/x^2$$
.

(10%)

Solve the following initial value problems.

$$y'' + 2y' + 10y = 17\sin x - 37\sin 3x$$
,  $y(0) = 6.6$ 

$$v(0) = 6.6$$

$$y'(0) = -2.2$$

(15%)

3. Let 
$$\mathbf{A} = \begin{bmatrix} 6 & -2 & -2 \\ 10 & -3 & 1 \\ -10 & 5 & 1 \end{bmatrix}$$
,  $\mathbf{B} = \begin{bmatrix} 9 & 4 & -4 \\ 4 & 7 & 0 \\ -4 & 0 & 11 \end{bmatrix}$ , and  $\mathbf{a} = \begin{bmatrix} 5 \\ 1 \\ 2 \end{bmatrix}$ ,

please calculate AB,  $A^{T}A$ ,  $(A^{T})^{2}$ ,  $a^{T}Aa$ ,  $a^{T}(A+A^{T})a$ 

(15%)

Find a basis of eigenvectors and diagonalize the following matrix

$$\begin{bmatrix} -1 & -1 & 0 \\ -1 & -1 & 0 \\ 0 & 0 & 2 \end{bmatrix} \tag{15\%}$$

Find the Fourier cosine series as well as Fourier sine series of the following function.

$$f(x) = \sin x \,, \qquad (0 < x < \pi)$$

(15%)

6. Find eigenvalues and eigenfunctions of the following problem.

$$y'' + \lambda y = 0$$
  $y(0) = y(1)$   $y'(0) = y'(1)$ 

(15%)

Using Laplace transform, solve the following integral equation

$$y(t) + \int_{0}^{t} y(\tau)d\tau = 2$$

(15%)

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