

國立中央大學104學年度碩士班考試入學試題

所別：地球科學系地球物理碩士班 不分組(一般生)

科目：普通物理學

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本科考試禁用計算器

*請在答案卷(卡)內作答

參考用

(一) Heat (共25分)

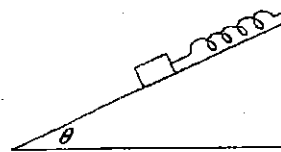
1. **Heat flow** (熱流) is the rate of heat energy transfer through a given surface, per unit surface and per unit second. What is the relationship between heat flow, temperature, and thermal conductivity? (10分)
2. Along a metal bar, the temperature is $T(x)=x^2$ at distance x in cm along the bar, and that the heat flow is 100 J/s at $x=200$ cm, what is the constant of proportionality. (15分)

(二) Rotation (共 25 分)

1. What is parallel axis theorem? (10 分)
2. 若地球對自轉軸的轉動慣量為 kMR^2 ，其中 M 為地球質量、 R 為地球半徑。由於潮汐對海岸的摩擦作用，地球自轉的速度逐漸減小，每 1000 萬年周期增加 400 秒，求潮汐對地球的平均力矩多大？(8分) 地球動能的減小相當於摩擦消耗多大的功率？(7分)

(三) Simple harmonic motion and friction (共 25 分)

A block of mass m rests on an incline which makes an angle θ with the horizontal plane (see the right figure). There is friction between the block and the surface. The static friction coefficient μ_s is larger than the kinetic friction coefficient, μ_k . The block is attached to a "massless" spring of spring constant k . In the absence of any forces on the spring, its (relaxed) length would be l .



- (1) We pull on the block and extend the spring till its length is $l+x$. What is the maximum extension, x_{max} , of the spring for which the block will remain stationary when released? (5 分)
- (2) In this position, show a free body diagram for the block. Indicated all forces that act on the block and give their magnitude. (5 分)

In the following three questions, use the symbol x_{max} .

- (3) In this position, the block is then gently touched at time $t=0$. It starts moving. For what value of x will the block reach its maximum speed? (5 分)
- (4) As the block moves, the spring will get shorter. At some point in time, t_1 , the extension is x . How much work was done by (i) gravity, (ii) the spring force, and (iii) by the friction between $t=0$ and t_1 . (5 分)
- (5) As the block moves up-hill, the spring gets shorter. What is a necessary requirement for the spring to become at least as short as its relaxed length l ? (5 分)

(四) Magnetic field (共25分)

- (1) What is Biot-Savart law (10 分)
- (2) Two wires, both of length L , are formed into a circle and a square, and each carries current i . Show that the square produces a greater magnetic field at its center than the circle produces at its center. (15 分)