

參考用

(10%) 1. X and Y are two independent random variables. X and Y have means and variances given as: $E(X) = 1$, $E(Y) = 2$, $\text{Var}[X] = 3$, $\text{Var}[Y] = 4$.

- (a) Compute $\text{Var}[2X - 3Y - 1]$.
- (b) Compute $\text{Var}[XY]$.
- (c) Compute correlation coefficient $\rho(Y - X, Y + X)$.

(15%) 2. The $\text{sgn}(f)$ function is defined as: $\text{sgn}(f) = \begin{cases} 1, & f > 0 \\ 0, & f = 0 \\ -1, & f < 0 \end{cases}$ and has the Fourier transform pair

$\frac{j}{\pi t} \Leftrightarrow \text{sgn}(f)$. Let $x(t)$ be the input signal to the filter $h(t) = \frac{1}{\pi t}$, and the output signal is represented as

$\hat{x}(t) = x(t) * h(t)$, where $*$ denotes the convolution operation. If $y(t) = x(t) \cos(\omega_0 t) + \hat{x}(t) \sin(\omega_0 t)$:

- (a) Please express the spectrum $Y(f)$ of $y(t)$ in terms of f_0 , $X(f)$ and $\text{sgn}(f)$, where $X(f)$ is the spectrum of $x(t)$, which is lowpass with the bandwidth $B < f_0 = \frac{\omega_0}{2\pi}$.
- (b) Sketch $Y(f)$ if $X(f)$ is shown as in Figure 1.

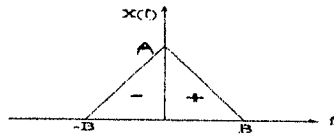


Figure 1

(15%) 3. An FM modulator has output: $x_c(t) = 50 \cos[\omega_c t + 2\pi f_d \int^t m(\alpha) d\alpha]$, where $f_d = 25\text{Hz/V}$. Assume

that $m(t)$ is the signal equal to $2\Pi[\frac{1}{4}(t-2)] + 4\Pi[\frac{1}{2}(t-6)]$, where $\Pi(t) = \begin{cases} 1 & |t| < \frac{1}{2} \\ 0 & \text{otherwise} \end{cases}$

- (a) Determine the peak frequency deviation in hertz.
- (b) Determine the peak phase deviation in radians.
- (c) Determine the power at the modulator output.

(10%) 4. Consider the system: $x(t) \rightarrow \oplus \rightarrow \frac{\partial}{\partial t} \rightarrow \boxed{\text{Lowpass filter}} \rightarrow y(t)$. The signal $x(t)$ is defined by

$x(t) = A \cos(2\pi f_c t)$. The lowpass filter has unit gain in the passband and bandwidth W , where $f_c < W$. The noise $n(t)$ is white with two-sided power spectral density $N_0/2$. The signal component of $y(t)$ is defined to be the component at frequency f_c . Determine the signal-to-noise ratio of $y(t)$.

注意: 背面有試題

系所別: 通訊工程學系 甲組 科目: 通訊系統

(30%) 5. 有 3 個銅板，假設第 1、2、3 個銅板是正面的機率分別是 $1/3$ 、 $1/3$ 、 $1/2$ 。今告知您下列資訊，請問第 3 個銅板是正面的機率為多少？

請在下列答案中選出適當項目號碼，每小題答錯不倒扣，答案若為其它請寫出應該多少。

項目號碼	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
答案	$1/2$	$1/3$	$1/4$	$1/5$	$1/6$	$1/7$	$1/8$	$1/9$	其它

- a). 全部銅板都是一樣花色(即正面或反面)。
- b). 有偶數個正面(包含零個)。
- c). 有 1 個正面、2 個反面。

(10%) 6. We have two hypotheses for the observed data Z

Hypotheses H_0 $Z = N$ (noise alone) $\Pr(H_0 \text{ true})=1/4,$

Hypotheses H_1 $Z = k + N$ (signal plus noise) $\Pr(H_1 \text{ true})=3/4.$

Assume that the noise N is an added white Gaussian noise with zero mean and variance σ^2 . And k is a constant.

Use the Bayes' criterion to find the threshold of Z for deciding whether Z belongs H_1 or H_0 .

請在下列答案中選出適當項目號碼，答錯不倒扣，答案若為其它請寫出應該多少。

項目號碼	(1)	(2)	(3)	(4)	(5)	(6)	(7)
答案	$\frac{k}{2}$	$\frac{k - \sigma^2}{2k} \ln 3$	$\frac{k - \sigma^2}{3k} \ln$	$\frac{k}{3}$	$\frac{k - \sigma^2}{2k} \ln 2$	$\frac{k - \sigma^2}{3k} \ln 3$	其它

(10%) 7. 有一接收機，其工作方式為：連續收 4 個位元(bits)才決定訊號是 1 或 0；其判斷方法是：若 4 個位元中至少有 2 個 1，則決定訊號是 1，否則為 0。若假設每個位元是 1 的機率為 0.6，問此接收機決定訊號是 0 的機率為多少？

請在下列答案中選出適當項目號碼，答錯不倒扣，答案若為其它請寫出應該多少。

項目號碼	(1)	(2)	(3)	(4)	(5)	(6)	(7)
答案	0.2388	0.1928	0.1842	0.1768	0.1792	0.1898	其它

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