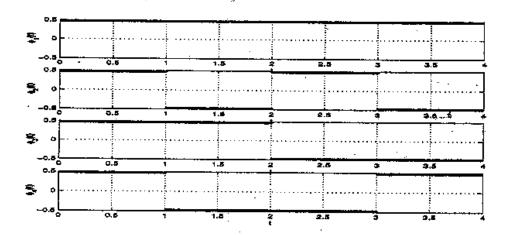
國工中央大学九十学年度領士班研究生入學試題卷

所別: 電機工程學系 丁組 科目: 通訊系統 共 2 頁 第 1 頁

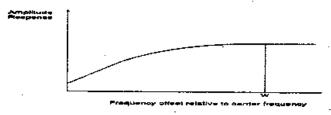
- 請從六個試題中選五題作答。若作答六題,以得分較低的五題計分。
- 1. Consider the set of four functions $\phi_1(t)$, $\phi_2(t)$, $\phi_3(t)$, and $\phi_4(t)$ shown below. The signal

$$x(t) = \begin{cases} 4t, & 0 \le t \le 4 \\ 0, & otherwise \end{cases}$$

- (a) Find the expression for $x_a(t)$ over the interval $0 \le t \le 4$ in terms of $\phi_1(t), \phi_2(t), \phi_3(t),$ and $\phi_4(t)$, (i.e., $x_a(t) = \alpha_1 \phi_1(t) + \alpha_2 \phi_2(t) + \alpha_3 \phi_3(t) + \alpha_4 \phi_4(t)$) such that the intergral squared error $\epsilon_N = \int_0^4 ||x(t) x_a(t)||^2 dt$ (ISE) is minimized. [15 pts.]
- (b) Calculate the minimium ISE, [5 pts.]



- 2. We have a FM signal: $x_c(t) = A_c \cos[2\pi f_c t + \phi(t)]$, where $\phi(t) = 30\pi \int_0^t 4\sin(40\pi\alpha) d\alpha$, and $f_c = 1000Hz$
 - (a) Find the value of the modulation index [5 pts.]
 - (b) What is the reason we use the deemphasis filter in the FM demodulation? [5 pts.]



- (c) If we have the response of a deemphais filter as the above (W is the bandwidth of the message), how do you design your preemphasis filter (Draw the amplitude response of the preemphasis filter approximately)? Explain your design. [5 pts.]
- (d) What is the threshold effect in the FM discriminator? Explain briefly why the frequency-compressive feedback loop can be used for the threshold extension. [5 pts.]
- 3. The output of an operational amplifier is

$$Y = a_1 X_1 + a_2 X_2 + a_3 X_3,$$

where X_i , i = 1, 2, 3, are inputs and a_i are some constants.

(Case 1) If X_i are independently Gaussian distributed with means $\mathbb{E}[X_i] = m_i$ and variances $\text{Var}[X_i] = \sigma_i^2$.

(Case 2) If X_i are independently Poisson distributed with the probability mass functions

$$\Pr(X_i = k) = \frac{\Lambda_i^k e^{-\Lambda_i}}{k!}, \quad k = 0, 1, 2, 3, ...$$

Find the distribution of Y for both cases. [20 pts.]

注:背面有試題

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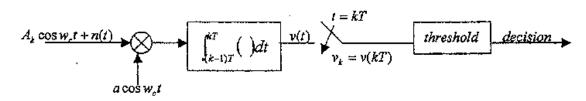
4. The random variable Y is Gaussian distributed with mean 0 and variance 1. Y is processed through a shaper.

(Case 1) The output of the shaper is $Z = \tanh Y$. (Note: tanh denotes hyperbolic tangent function.)

(Case 2) The output of the shaper is $Z = Y^2$.

Find the distribution of Z for both cases. [20 pts.]

- 5. Consider the coherent receiver shown below. The received signal is $A_k cos \omega_c t + n(t)$, where n(t) is a zero-mean white Gaussian noise with double-sided power spectral density $\frac{N_0}{2}$. The amplitude A_k carries the information bit at time k. Let v_k denote the output of the sampler at time k, and T denote the signalling interval. Assume that $\omega_c = \frac{2\pi m}{2}$, m is an integer.
 - (a) If $A_k \in \{A, -A\}$, and the value of a is chosen such that v_k is equal to 1 + N or -1 + N, where N is a zero-mean random variable. Let $\sigma^2 = E\{N^2\}$, (where $E\{\}$ is the expectation operator). Represent $\frac{E_k}{N_0}$ in terms of σ , where E_k denote the energy per symbol. [10 pts.]
 - (b) The function of the "threshold" box is to decide the value of A_k . If $A_k \in \{A, -\frac{4}{2}\}$ and a = 2, what is the error probability with the optimum threshold? (Use Q or erfc functions.) [10 pts.]



- 6. Consider the noncoherent receiver shown below. Let x_k and y_k denote the outputs of the samplers at time k. Let T denote the signalling interval. Assume that $\omega_c = \frac{2\pi m}{T}$, m is an integer.
 - (a) Represent $E\{x_k\}$ and $E\{y_k\}$ in terms of A, ϕ_k, θ and T (where $E\{\}$ is the expectation operator). [10 pts.]
 - (b) Assume that θ is a constant and unknown at the receiver. Let ϕ_k denote the modulation phase at time k and $\phi_k = (\phi_{k-1} + \Delta \phi_k) \mod 2\pi$, where $\Delta \phi_k$ is the data phase at time k. Assume that $\Delta \phi_k \in \{-\frac{\pi}{2}, 0, \frac{\pi}{2}\}$. In the "decision logic" box, the test statistic is used to detect the value of $\Delta \phi_k$. There are two possible test statistics: $l_1 = x_k x_{k-1} + y_k y_{k-1}$ and $l_2 = x_k y_{k-1} y_k x_{k-1}$. Which test statistic is suitable? Explain the reason. [10 pts.]

