

國立中央大學100學年度碩士班考試入學試題卷

所別：太空科學研究所碩士班 不分組(一般生)

科目：近代物理

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本科考試禁用計算器

\*請在試卷答案卷(卡)內作答

1. A satellite that orbits Earth (the radius of 6400km) in a circle with a period of 12 hours, the height of its orbit is 20200km and emits radio waves at a frequency of 1.5GHz. The angle between the direction of the motion of the satellite and the direction from it to a receiver is 90degrees.
  - (a) If the receiver is fixed on the ground. What frequency change is found by the receiver? (5%)
  - (b) If the receiver on car moving at 200km/hour. What frequency change is found by the receiver? (5%)
  - (c) What is the time difference between a clock in the satellite and one on the ground after 7200 circulations of the satellite? (5%)
  - (d) What is the phase difference between the emitted radio waves and the received waves after 2 circulations of the satellite? (5%)
  - (e) The satellite has a mass of 200kg on the ground. What is the angular momentum of the satellite? (5%)
2. Photometers measure light by counting individual photons. Does the principle of photometers associate with the photon process of
  - (a) the photoelectric effect? Why? (5%)
  - (b) the Compton effect? Why? (5%)
  - (c) the pair production? Why? (5%)
3. A particle has momentum  $p = mv$  with the relativistic mass  $m$ . We describe its state by using a de Broglie wave.
  - (a) What the group velocity is it associated with the velocity? (5%)
  - (b) What the phase velocity is it associated with the velocity? (5%)
  - (c) How can the phase velocity physically be greater than the speed of light  $c$ ? (5%)
4. In one-dimensional space, a particle having energy  $E$  approaches a potential barrier of width  $L$  and height  $V$ .
  - (a) Draw the wave function distribution for  $E > V$ . (5%)
  - (b) Is there a situation in which the transmission probability is 1? Why? (5%)
  - (c) Why the tunneling effect is observed only on the atomic scale? (5%)
5. A quantum particle of mass  $m$  moves in a circle of radius  $a$ .
  - (a) What is its wave equation? (5%)
  - (b) Find the possible energies of the particle. (5%)
  - (c) Find the possible angular momentum of the particle. (5%)
6. A hydrogen atom is in a state with quantum numbers, the principal quantum number  $n = 4$  and the orbital quantum number  $l = 3$ .
  - (a) What are the possible values of the total angular momentum quantum number  $j$ ? (5%)
  - (b) What are the possible  $z$  components of the total angular momentum? (5%)
7. Why does the total energy of a Fermi-Dirac system not approach zero as temperature  $T \rightarrow 0$ ? (5%)

參考用