

國立中央大學100學年度碩士班考試入學試題卷

所別：電機工程學系碩士班 固態組(一般生) 科目：半導體元件 共 1 頁 第 1 頁

本科考試禁用計算器

\*請在試卷答案卷(卡)內作答

1. The lattice constant of a simple cubic cell is  $a$ . (a) (5%) Calculate the distance between the nearest parallel (110) planes. (b) (5%) Calculate the surface density of atoms on the plane (110).
2. (10%) Calculate the electron diffusion current density. Assume that the electron mobility is  $1000 \text{ cm}^2/\text{V}\cdot\text{s}$  at  $kT/q = 0.026 \text{ V}$ ,  $q = 1.6 \times 10^{-19} \text{ C}$ , and  $\frac{dn}{dx} = 1 \times 10^{21} \text{ cm}^{-4}$ .
3. (10%) In a pn junction,  $N_a$  is the p-type doping density,  $N_d$  is the n-type doping density. The electric potential  $\phi(-x_p) = 0$ , and  $\phi(x_n) = V_{bi}$ ,  $x_p$  is the p-type depletion width, and  $x_n$  is the n-type depletion width. Both  $x_p$  and  $x_n$  are positive.  $V_{bi}$  is the built-in potential. If  $\phi(x) = a(x - x_n)^2 + V_{bi}$  for  $0 \leq x \leq x_n$ , find  $a$  in terms of  $N_d$ .
4. (10%) The total forward-bias current in a pn diode is the sum of the recombination and the ideal diffusion current densities as  $J = J_{rec} + J_D$ .  $J_D = J_s(\exp(\frac{V_a}{V_t}) - 1)$ .  $J_{rec} = J_{r0}(\exp(\frac{V_a}{2V_t}) - 1)$ .  $J_{r0} > J_s$ . Sketch  $\ln(J)$  versus  $\frac{V_a}{V_t}$  for  $V_a > 0$ . Show the  $\ln(J_{r0})$ ,  $\ln(J_s)$  on your plot.
5. Consider a Schottky barrier diode with n-type silicon doped to  $N_d$ . (a) (5%) Find the theoretical barrier height  $\phi_{B0}$  in terms of the metal work function  $\phi_m$  and the silicon electron affinity  $\chi$ . (b) (5%) Find the built-in potential barrier  $V_{bi}$  in terms of the effective density of states in the conduction band  $N_c$ .
6. Consider an npn transistor with a base region from  $x = 0$  to  $x_B$ . The excess electron concentration  $\Delta n_B(x) = \Delta n_B(0) = \Delta n_{B1}$  at  $x = 0$ .  $\Delta n_B(x) = \Delta n_B(x_B) = \Delta n_{B2}$  at  $x = x_B$ .  $\Delta n_{B1} > 0$  and  $\Delta n_{B2} < 0$  (a) (5%) Plot  $\Delta n_B(x)$  versus  $x$  if  $x_B \gg L_B$ , where  $L_B$  is the electron diffusion length in the base region. (b) (5%) If  $\Delta n_B(x) = m_1 \cdot \Delta n_{B1} + m_2 \cdot \Delta n_{B2}$  for  $x_B \ll L_B$ , find  $m_1$  and  $m_2$  in terms of  $x$  and  $x_B$ .
7. (a) (5%) Sketch the basic Ebers-Moll equivalent circuit for an npn bipolar transistor with the following parameters:  $\alpha_F$ ,  $\alpha_R$ ,  $I_{ES}$ ,  $I_{CS}$ ,  $V_{BE}$ , and  $V_{BC}$ . (b) (5%) The Ebers-Moll model has four parameters:  $\alpha_F$ ,  $\alpha_R$ ,  $I_{ES}$ , and  $I_{CS}$ . According to the reciprocity relationship, the four parameters can be reduced to three independent parameters:  $\alpha_F$ ,  $\alpha_R$ , and  $I_S$ . Find  $I_S$  in terms of  $\alpha_F$  and  $I_{ES}$ .
8. (10%) Using superposition, the shift in the flat-band voltage due to a fixed constant charge distribution  $\rho(x) = \rho_1$  in the oxide region can be given by  $\Delta V_{FB} = a\rho_1 t_{ox}^2$ . Find the expression of  $a$  in terms of  $\epsilon_{ox}$ , where  $\epsilon_{ox}$  is the permittivity of the oxide, and  $t_{ox}$  is the oxide thickness.
9. (a) (5%) Sketch the C-V characteristics of an MOS capacitor with a p-type substrate under the low-frequency condition and the high-frequency condition in a same plot. (b) (5%) Sketch the differential charge distributions under the low-frequency condition and the high-frequency condition respectively.
10. (10%)  $I_D = \frac{W\mu_n C_{ox}}{2L} [2(V_{GS} - V_T)V_{DS} - V_{DS}^2]$  for an n-channel MOSFET in the nonsaturation region. Describe how to determine the inversion carrier mobility  $\mu_n$  and the threshold voltage  $V_T$  from the I-V experimental results. For a fixed  $V_{DS}$ ,  $I_D = I_{D1}$  if  $V_{GS} = V_{GS1}$ , and  $I_D = I_{D2}$  if  $V_{GS} = V_{GS2}$ .