

1. (A) In Stokes region ( $Re < 0.1$ ), the drag coefficient  $C_D$  is equal to  $Re/24$ . Derive an expression which can be used to determine the terminal settling velocity of a spherical particle settling in air in this region. Define all the terms you use. (15%)
- (B) Use the expression you derived in Part (A) to calculate the terminal settling velocity of a spherical particle with a diameter of  $6.0 \mu\text{m}$  settling in air at 1 atm and 300 K. The particle's density is  $2.5 \text{ g/cm}^3$ . The density and viscosity of air are  $1.18 \text{ kg/m}^3$  and  $0.0666 \text{ kg/m hr}$ , respectively. Please check the validity of your result. (15%)
2. Consider the two dimensional incompressible flow which can be specified by  
 $u = ky, \quad v = kx, \quad w = 0$ , where  $k$  is a constant.
- (A) Show that this flow field satisfies the continuity equation. (5%)  
 (B) Sketch the streamlines for the flow field. (10%)
3. Oil is to be pumped at a rate of at least 6 liters/min through a horizontal pipe of length 300 m. The pump has a discharge pressure of 200 kN/m<sup>2</sup> absolute. The pipe discharges into an open tank containing oil to a depth of 8 m above the inlet. If the oil has density of  $800 \text{ kg/m}^3$  and a viscosity of  $0.004 \text{ N s/m}^2$ . What diameter pipe would you recommend? If any assumption regarding laminar or turbulent flow is made, prove your assumption is valid. (15%)
4. Explain the following terms: (20%)
- Navier-Stokes Equation
  - characteristic curves for a pump
  - Manning formula
  - Froude number
  - ideal fluid
5. A vertical Venturi meter is used to measure the flowrate of a petroleum product. The product is flowing in a 150 mm diameter pipeline and the Venturi meter has a throat diameter 110 mm. Pressure tappings are placed at the throat and a height of 400 mm above the throat. A mercury filled U tube manometer is connected to the pressure tappings. What is the difference in the mercury levels on the manometer if the flowrate of the petroleum products is  $0.05 \text{ m}^3/\text{s}$ ? (20%)
- Relevant Data:
- Density of the petroleum product =  $830 \text{ kg/m}^3$
  - Density of mercury =  $13600 \text{ kg/m}^3$
  - The venturi discharge coefficient = 0.98