

國立中央大學八十四學年度碩士班研究生入學試題卷

所別: 太空科學研究所

組 科目: 電磁學

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1. A point charge q with mass m moves inside a region with uniform fields.

$$\vec{B} = B\hat{z}, \quad \vec{E} = E\hat{y}.$$

Assuming its velocity \vec{v} is much less than the speed of light.

- (a) If the total force on the charge particle is zero, determine the trajectory of the particle. (5%)
(b) If the particle started from rest at the origin, determine the trajectory of the particle. (10%)

2. A spherical cavity of radius a is hollowed out from the interior of a perfect conducting sphere of radius R . The distance between the centers of the sphere and the cavity is d . A point charge q is placed at the center of the cavity.

- (a) Determine the induced charge distribution on the conductor. (10%)
(b) Determine the electric field everywhere. (10%)
(c) If there is another charge Q brought near the conductor. Does the charge Q act a force on the charge q in the cavity? (5%)

3. A dielectric sphere of radius R and permittivity ϵ is situated in a vacuum and is charged throughout its volume by a charge density $\rho(r) = \kappa r$, r being the distance from the center of the sphere. Find the energy of the configuration. (16%)

4. (16%)

- (a) Derive the boundary condition of \vec{H} at the interface between two different media.
(b) The \vec{H} field in air just above a perfect conductor is given by $\vec{H}_1 = 4\hat{x} + 3\hat{z}$ ampere per meter. Find the surface current \vec{J}_s on the surface of the perfect conductor. The conductor occupies the space $y < 0$.

5. (18%)

A uniform plane wave propagating in free space is characterized by the complex electric vector,

$$\vec{E} = (j3\hat{x} + 5\hat{y} - j4\hat{z})e^{j(\omega t - 0.2\pi(4x + 3z))}.$$

- (a) Find the equation of the plane of constant phase.
(b) Determine the frequency and wavelength.
(c) Find the magnetic field \vec{H} associated with the given \vec{E} .
(d) Find the average Poynting's vector.
(e) What is the polarization of the wave in the plane of constant phase.

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6. Use the conservation of energy to show that there are a reflected wave and a transmitted wave when a plane wave is incident normally on the interface between two different simple dielectric media. (10%).

參考用