

國立中央大學99學年度碩士班考試入學試題卷

所別：企業管理學系碩士班 一般丙組(一般生) 科目：統計學 共 / 頁 第 / 頁

一般丁組(一般生)

\*請在試卷答案卷(卡)內作答

企業電子化辛組(一般生)

\*本科考試禁用計算器

1. If we think of the sequence of items emerging from a manufacturing processes as defective ( $F$ ) or nondefective ( $S$ ), suppose that a sequence consists of  $n_1=5$   $S$  elements and  $n_2=3$   $F$  elements, find the probability of observing the number of runs  $R$  less than 4, i.e.  $\Pr(R < 4)$ . (15%)
2. The number of parking tickets issued in a certain street on any given weekday has a Poisson distribution with parameter  $\theta=50$ . What is the approximate probability that the total number of tickets given out during five-day week is between 225 and 275? (15%)
3. (a) What is the *observed* significant level? How to use it to conduct hypothesis testing. (10%)  
(b) Draw the *power curve* for testing the null hypothesis  $H_0: u=u_0$  vs  $H_a: u \neq u_0$  with significant level  $\alpha$ , discuss the situation at minimum testing power. (10%)  
(c) Propose at least one statistic to test the assumption of *homogeneity of variances* in One-way ANOVA. Provide an alternative approach to conduct further test if the assumption of homogeneity of variances does not hold. (10%)  
(d) Given two sample data  $\{n_1, \bar{x}_1, S_1^2; n_2, \bar{x}_2, S_2^2\}$ , what is the *degree of freedom*  $\nu$  of  $t$  statistic being used for the two-sample mean inference under the case on unequal variances? (5%)
4. Develop a linear regression model which may predict the weight( $W$ ) by height( $H$ ) for both female and male. State the assumptions given in your model. (15%)
5. Suppose that a manager wishes to compare the number of complaints per week filed by union stewards for two shifts at a manufacturing plant. One hundred independent observations on the number of complaints gave means  $\bar{x} = 20$  for shift 1 and  $\bar{y} = 22$  for shift 2. Assume that the number of complaints per week on the  $i$ -th shift has a Poisson distribution with a mean  $\theta_i$ ,  $i=1, 2$ . Test  $H_0: \theta_1 = \theta_2$  vs  $H_a: \theta_1 \neq \theta_2$  by the *likelihood ratio method*, with significant level 0.01. (20%)

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 $\Pr(0 \leq Z \leq 1.61) = 0.4463$   $\Pr(0 \leq Z \leq 3.5) = 0.4997$   $\Pr(Z \geq 4.5) = 0.000003$

$\chi^2_{.01,1} = 6.63$   $\chi^2_{.01,2} = 9.21$   $\ln(20) = 2.99573$   $\ln(21) = 3.04452$   $\ln(22) = 3.09104$

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