

# 國立中央大學八十六學年度碩士班研究生入學試題卷

所別： 大氣物理研究所

不分組 科目：

電磁學

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1. Consider the electric potential (in spherical coordinates)

$$\Phi = \frac{a \sin \theta}{r^2} + \frac{b}{r}$$

where  $a$  and  $b$  are constants.

- (a) Determine the electric field associated with this potential. (5%)  
(b) What is the charge distribution responsible for this potential. (10%)  
(c) Discuss the electrostatic energy for this charge distribution. (10%)
2. Two grounded conducting planes intersect at  $90^\circ$  and a point charge  $q$  lies between them.  
(a) Determine the electric potential and the electric field everywhere. (10%)  
(b) Determine the charge distribution on the planes. (5%)
3. A conducting spherical shell of radius  $R$ , carrying total charge  $Q$ , is set spinning at angular velocity  $\omega$  about the  $z$  axis.  
(a) What is the magnetic dipole moment of the spherical shell. (5%)  
(b) Find the vector potential everywhere. (10%)  
(c) Find the magnetic field inside and outside the sphere. (5%)
4. A square wire of width  $a$  in  $x$ - $y$  plane is moving parallel to its width at a uniform speed  $v$  in  $y$ -direction. A very long wire carrying a stationary current  $I$  along the  $x$ -direction, is at distance  $d$  from the nearest side of the square wire.  
(a) Determine the induced electromotive force (*emf*) in the square wire. (10%)  
(b) Determine the mutual inductance of the circuits. (5%)
5. For a monochromatic plane wave has electric amplitude  $E_0$ , angular frequency  $\omega$  and phase angle zero. If it is traveling in the  $y$ -direction and polarized in the  $z$ -direction.  
(a) Write down the electric and magnetic fields. (10%)  
(b) What are the energy density and the momentum density of the wave? (10%)  
(c) when it incident on a thick slab of conducting material, what happen? (5%)