國立中央大學九十三學年度碩士班研究生入學試題卷 共/頁 第/頁

所別: <u>太空科學研究所碩士班</u> 科目: 近代物理

- 1. Two events occur at points x_1 and x_2 at the same time t_0 in the inertial frame S, which moves with speed V relative to the inertial frame S.
- (a) What is the spatial separation of these events measured in S? (5%)
- (b) What is the time interval of these evens measured in S? (5%)
- 2. A gamma ray streaks through the lab at an angle of 60° with the +x direction (in the x-y plane of the lab). Compute the magnitude and direction of the gamma ray's velocity when viewed from frame S' moving with the relative speed V=0.6c along the +x direction. (10%)
- 3. The total energy of a particle is twice its rest energy. (a) Find the speed of the particle. (b) Find its momentum in terms of its rest energy. (10%)
- 4. By using Planck's law for the energy density distribution function $u(\lambda)$ of the radiation

in the cavity $u(\lambda) = \frac{8\pi h c \lambda^{-5}}{e^{hc/\lambda kT} - 1}$, find the temperature of a blackbody if its spectrum has its peak at (a) $\lambda_m = 3cm$, (b) $\lambda_m = 3m$. (10%) $h = 6.626 \times 10^{-34} J.s$, $k = 1.38 \times 10^{-23} J/K = 8.617 \times 10^{-5} eV/K$

- 5. For an electron with particle velocity v=0.8c, (a) show that the phase velocity of the electron wave is greater than c, (b) show that the group velocity of the electron wave equals the particle velocity of the electron. (10%)
- 6. (a) Show that the function $\varphi(x) = Ae^{-x^2/2a^2}$ represents the ground state of a harmonic oscillator with mass m in the potential $V(x) = \hbar^2 x^2 / 2ma^4$.
 - (b) Show that $a \frac{d\varphi(x)}{dx}$ is also an eigenstate of a harmonic oscillator.
 - (c) What is the energy of this new state? (15%)
- 7. Consider a particle moving in a two-dimensional space defined by $V(x, y) = V_0$ for 0 < x < L and 0 < y < L and $V = \infty$ elsewhere. (a) Write down the eigenstates for the particle in this well. (b) Find the expression for the corresponding energies. (10%)
- 8. Why doesn't the energy of the hydrogen atom depend on the orbital quantum? (5%)
- 9. A hydrogen atom is in a state with quantum numbers, principal quantum number n=3, orbital quantum number l=2. (a) What are the possible values of the total angular momentum quantum number j? (b) What are the possible values of the magnitude of the total angular momentum? (c) What are the possible z components of the total angular momentum? (15%)
- 10. Why does the total energy of the fermion gas not approach zero as temperature $T \rightarrow 0$? (5%)

