國立中央大學94學年度碩士班考試入學試題卷 共/頁 第/頁 所別:產業經濟研究所碩士班 甲組 科目:微積分

以下每題25分,可選擇以英文或中文作答。

- 1. Show that continuity is a necessary, but not a sufficient condition for differentiability.
- 2. Suppose that a wine dealer is in possession of a case of wine, which he can either sell at the present time (t=0) for a sum of K or else store for a variable length of time and then sell at a higher value. The growing value V of the wine is known to be the following function of time: $V = Ke^{\sqrt{t}}$. Assume that the interest rate r=0.1. Find the value of t that maximizes the present value of V. (Note: You should check both FOC and SOC.)
- 3. Let B be a closed convex set of points in n-dimensional euclidean space, and let $x=(x_1,\cdots,x_n)$ be a point not in B. Show that there exist numbers p_1,\cdots,p_n,p_{n+1} such that $\sum_{i=1}^n p_i x_i = p_{n+1}$ and $\sum_{i=1}^n p_i y_i > p_{n+1}$ for all $y \in B$.
- 4. Consider the CES production function, $Q = A[\delta K^{-\rho} + (1-\delta)L^{-\rho}]^{-1/\rho}$, where A > 0, $0 < \delta < 1$, $-1 < \rho \neq 0$. Show that the function satisfies Euler's theorem (i.e., $K\frac{\partial Q}{\partial K} + L\frac{\partial Q}{\partial L} = Q$).