## 國立中央大學 107 學年度碩士班考試入學試題

所別: 電機工程學系碩士班 固態組(一般生)

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科目: 半導體元件

本科考試禁用計算器

\*請在答案卷(卡)內作答

1. (5%) (a) At 300 K, the lattice constant for Si is 0.543 nm, Calculate the number of Si atoms per cubic nanometer.

(5%) (b) What is the distance between nearest neighbors in Si? Give your answer in nm.  $\sqrt{2} = 1.732$ .

2. (4%)(a) If the continuity equation for hole is  $\frac{\partial p}{\partial t} = c_1 \frac{\partial J_p}{\partial x} + (G_p - R_p)$ ,  $J_p$  is the hole current density,  $G_p$  is the hole generation rate, and  $R_p$  is the hole recombination rate. Find the expression for  $c_1$ .

(3%)(b) Assuming an n-type sample under uniform illumination, the continuity equation for hole in (a) can be used to find  $p_n(t)$ .  $R_p = \frac{p_n - p_{no}}{\tau_p}$ ,  $\tau_p$  is the hole life time. In steady state (t < 0),  $\frac{\partial p_n}{\partial t} = 0$ , and for uniform distribution,  $\frac{\partial^2 p_n}{\partial x^2} = 0$ , and  $G_p = G_L$ , find  $p_n(t)$  for t < 0.

(3%)(b) At t = 0, the light is turned off. Find  $p_n(t)$  for  $t \ge 0$ .

3. Consider a silicon pn junction with doping concentrations of  $N_a=1\times 10^{17}~\rm cm^{-3}$  and  $N_d=2\times 10^{17}~\rm cm^{-3}$ . Assume  $V_{bi}=V_{bi}^p+V_{bi}^n$ ,  $W=x_p+x_n$ .  $V_{bi}^p$  is the built-in voltage across the p-side of the junction, and  $x_p$  is the depletion width across the p-side of the junction.

(5%)(a) If  $V_{bi}^p = V_{bi}/(1+r_1)$ , calculate  $r_1$ .

(5%)(b) If  $x_n = W/(1 + r_2)$ , calculate  $r_2$ .

4. For steady state and electric field E=0, the excess minority carrier hole concentration  $\delta p(x)$  in the n region is determined from with  $\delta p(0)=c_1$ , and  $\delta p(x_B)=c_2$ . (10%) (a) If  $\delta p(x)=Ae^{sx}+Be^{-sx}$ , find s. If  $A=\frac{f_1}{2\sinh(\frac{x_B}{L_p})}$ , and  $B=\frac{f_2}{2\sinh(\frac{x_B}{L_p})}$ , find  $f_1$  and  $f_2$ .

(5%) (b) If  $\delta p(x) = f_3 \cdot \sinh(\frac{x_B - x}{L_n}) + f_4 \cdot \sinh(\frac{x}{L_n})$ , find  $f_3$  and  $f_4$ .

(5%) (c) If  $\frac{x_B}{L_p} \to 0$ , and  $\delta p(x) = f_5 \cdot \frac{x_B - x}{x_B} + f_6 \cdot \frac{x}{x_B}$ , find  $f_5$  and  $f_6$ .

5. Consider a p-type silicon substrate doped to  $N_a = 1 \times 10^{16} \text{ cm}^{-3}$ . The oxide is silicon dioxide with a thickness of  $t_{ox} = 18 \text{ nm}$ . Note that kT/q = 0.026 V,  $n_i = 1 \times 10^{10} \text{ cm}^{-3}$ ,  $E_g = 1.12 \text{ eV}$ , the electron affinity X = 4.01 V,  $\epsilon_{Si} = 11.7 \times 8.85 \times 10^{-14} \text{ F/cm} = 103.5 \times 10^{-14} \text{ F/cm}$ ,  $\epsilon_{ox} = 3.9 \times 8.85 \times 10^{-14} \text{ F/cm} = 34.5 \times 10^{-14} \text{ F/cm}$ ,  $q = 1.6 \times 10^{-19} \text{ C}$ ,  $\epsilon_{Si}/q = 64.7 \times 10^5 \text{ 1/V·cm}$ , and  $\ln(10^6) = 13.8$ . (7%) (a) If the gate is  $n^+$ -polysilicon, find the threshold voltage  $V_{Ta}$ .

(3%) (b) If the gate is  $p^+$ -polysilicon, the threshold voltage is  $V_{Tb}$ . Find the value  $V_{Tb} - V_{Ta}$ .





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6. (4%) (a) Consider an n-channel MOSFET with the channel width  $W=1~\mu\mathrm{m}$ . The inversion charge  $|Q'_n| = 10^{-6} \text{ C/cm}^2$ , the electron velocity is  $10^6 \text{ cm/s}$ . Calculate the channel current  $I_D$ .

(3%) (b) If  $|Q'_n(y)| = C_{ox}(V_{GS} - V_T - V(y))$ , the electron velocity  $|v_n(y)| = \mu_n \frac{dV(y)}{dy}$ ,

and  $I_D(y) = f_1 \cdot (V_{GS} - V_T - V_y) \frac{dV_y}{dy}$ , find  $f_1$ . (3%) (c) At y = L,  $V(y) = V_{DS}$ , y = 0, V(y) = 0. Assuming  $I_D(y) = I_D$  at any y, and  $\mu_n$  is constant, find  $I_D$  for  $(V_{GS} - V_T - V_{DS}) \ge 0$ .

7. (10%) Assume the following transistor parameters: the base doping  $N_B = 1 \times 10^{15}$ cm<sup>-3</sup>, the emitter doping  $N_E = 1 \times 10^{17}$  cm<sup>-3</sup>, the diffusion coefficient in the emitter  $D_E = 10 \text{ cm}^2/\text{s}$ , the diffusion coefficient in the base  $D_B = 20 \text{ cm}^2/\text{s}$ , the base width  $x_B = 0.6 \ \mu \text{m}$ , and the emitter width  $x_E = 0.8 \ \mu \text{m}$ . The minority carrier diffusion length in the base,  $L_B = 10.0 \ \mu \text{m}$ .  $x_B << L_B$  and  $x_E << L_E$ . Find the emitter injection efficiency  $\gamma$ , the base transport factor  $\alpha_T$ , and the common-emitter current gain  $\beta$ .

8. In an npn Ebers-Moll model,  $V_{BE}$  and  $V_{BC}$  can be obtained as functions of  $I_C$ ,  $I_B$ ,  $I_{ES}$ ,  $I_{CS}$ ,  $\alpha_F$ , and  $\alpha_R$ .

(5%) (a) If  $V_{BE} = V_t \cdot \ln(\frac{f_1+t_1}{t_1})$ , find  $f_1$ . Note that  $t_1 = I_{ES}(1-\alpha_F\alpha_R)$ , and  $V_t = kT/q$ .

(5%) (b) If  $V_{BC} = V_t \cdot \ln(\frac{f_2 + t_2}{t_2})$ , find  $f_2$ . Note that  $t_2 = I_{CS}(1 - \alpha_F \alpha_R)$ .

9. (5%) (a) The hybrid-pi ac model for an npn bipolar transistor is shown in Fig. 1. Assume  $i_b = g_{11}v_{be} + g_{12}v_{ce}$ , and  $i_c = g_{21}v_{be} + g_{22}v_{ce}$ . If  $g_{11} = \frac{\partial x}{\partial v}|_z$ , find x, y, and z. (5%) (b) Find  $r_{\pi}$  and  $g_{m}$ , which are functions of  $g_{11}$ ,  $g_{12}$ ,  $g_{21}$ , and  $g_{22}$ .

