

國立中央大學通訊工程學系 102 學年度碩士在職專班入學筆試

【通訊概論】試卷

考試地點：通訊館一樓 E1-109 室

考試時間：100 分鐘

試題總分：100 分

- Plot the time-domain waveforms of the following signals which are expressed in terms of the rectangular function  $\Pi(x) = \begin{cases} 1, & -0.5 \leq x \leq 0.5 \\ 0, & \text{otherwise} \end{cases}$  : (a)  $h(t) = \Pi\left(\frac{t}{2T}\right)$  ; (b)  $x(t) = \Pi\left(\frac{t}{2T}\right) - \Pi\left(\frac{t-2T}{2T}\right)$ ; (c)  $y(t) = \Pi(t) * \Pi(t) = \int_{-\infty}^{\infty} \Pi(t-\tau) \cdot \Pi(\tau) d\tau$ ; (15%)
- For a sinusoidal message signal  $m(t) = 2 \cdot \cos(2\pi \cdot f_0 \cdot t)$  with  $f_0 = 10^3$  Hz, (a) what is the period of the message signal; (b) what is the amplitude of the message signal; (c) what is the type of modulation when the transmitted signal is given by  $x(t) = m(t) \cdot \cos(2\pi f_c t)$  ( $f_c = 10^5$  Hz); (d) what is the type of modulation when the transmitted signal is given by  $x(t) = (4 + m(t)) \cdot \cos(2\pi f_c t)$ ; (e) what is the type of modulation when the transmitted signal is given by  $x(t) = 2 \cdot \cos\left(2\pi f_c t + 2\pi f_d \cdot \int_{-\infty}^t m(\tau) d\tau\right)$  ( $f_d = 10^3$  Hz). (25%)
- Find the correctness of the following statements or equations by answering right or wrong: (for example:  $2 > 1$ , the answer is wrong) (40%)
  - $2 \cos(2\pi f_c t) \cdot \cos(2\pi f_0 t) = \cos(2\pi(f_c + f_0)t) + \cos(2\pi(f_c - f_0)t)$ ;
  - the Gaussian probability density function with mean  $m_n \neq 0$  and variance  $\sigma_n^2$  is given by  $f_N(n_0) = \frac{1}{\sqrt{2\pi \cdot \sigma_n^2}} \exp\left(\frac{-n_0^2}{2\sigma_n^2}\right)$ ;
  - $\frac{1}{\sqrt{2\pi \cdot \sigma_n^2}} \int_0^{\infty} \exp\left(\frac{-n_0^2}{2\sigma_n^2}\right) \cdot dn_0 = 0.5$ ;
  - $\int_0^{\infty} \exp\left(\frac{-n_0^2}{2\sigma_n^2}\right) \cdot dn_0 > \int_{2\sigma_n^2}^{\infty} \exp\left(\frac{-n_0^2}{2\sigma_n^2}\right) \cdot dn_0$ ;
  - $\text{Re}\left\{(s_I(t) + j \cdot s_Q(t)) \cdot e^{j2\pi f_c t}\right\} = s_I(t) \cdot \cos(2\pi f_c t) + s_Q(t) \cdot \sin(2\pi f_c t)$ ;
  - the maximum data transmission rate (bps) of the Wi-Fi (802.11a) is higher than that of the USB 2.0 (Universal Serial Bus);

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(g) for a random variable  $X$  with a probability density function  $f_X(x)$ , the mean of  $X$  is

$$\text{given by } E[X] = \int_{-\infty}^{\infty} x \cdot f_X(x) dx;$$

(h) for two signals  $x_1(t) = \cos(2\pi \cdot 1000 \cdot t)$  and  $x_2(t) = \cos(2\pi \cdot 21000 \cdot t)$ , we have

$$x_1(n \cdot T_s) = x_2(n \cdot T_s) \text{ when } T_s = \frac{1}{10000};$$

(i) Mbps is the acronym (縮寫) of megabits per second;

(j) AWGN is the acronym of asynchronous window general network;

(Hint:  $e^{j2\pi f_c t} = \cos(2\pi f_c t) + j \cdot \sin(2\pi f_c t)$ ,  $\text{Re}\{e^{j2\pi f_c t}\} = \cos(2\pi f_c t)$ )

4. Find the wrong statement (only one) in the following statements: (4%)

(a) 3G mobile communication system use CDMA technology;

(b) DVB-T digital video broadcast system use OFDM technology;

(c) 3G mobile communication system use Turbo Convolutional coding;

(d) AGC is the acronym of Automatic Gain Control;

(e) Bluetooth use the OFDM technology.

5. Find the wrong equation (only one) in the following equations: (4%)

(a)  $\text{var}(x) = E[X^2] - (E[X])^2$  (the variance of a random variable  $X$ );

(b)  $X(f) = \mathfrak{F}\{x(t)\} = \int_{-\infty}^{\infty} x(t) \cdot e^{-j2\pi \cdot f \cdot t} dt$  (the Fourier transform);

(c)  $X(\omega) = DTFT\{x[n]\} = \sum_{n=-\infty}^{\infty} x[n] \cdot e^{j2\pi \omega n}$  (the discrete-time Fourier transform);

(d)  $y(t) = h(t) * x(t) = \int_{-\infty}^{\infty} h(t-\tau) \cdot x(\tau) d\tau = x(t) * h(t)$  (Linear convolution);

(e)  $Y(f) = \mathfrak{F}\{y(t) = h(t) * x(t)\} = \mathfrak{F}\{x(t)\} \cdot \mathfrak{F}\{h(t)\}$ .

6. Explain the following terms: (12%)

(a) Code-division multiplexing;

(b) OFDMA;

(c) dBm.