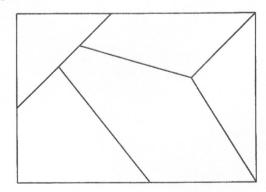
## 附件2:台灣聯合大學系統94學年度學士班轉學生考試命題紙

## 科目 龍散數學 類組別 D9 共一頁第一頁 \*請在試卷答案卷(卡)內作答

- 1. (10 points) The power set P(A) of set A is the set of all possible subsets of A. Justify the following statements by proving or disproving them:
  - (a) A, B are arbitrary sets, then  $P(A \cap B) = P(A) \cap P(B)$ .
  - (b) Given that  $A = \{a, \{a\}\}$ , then  $\{\{a\}\} \in P(A)$  and  $\{\{a\}\} \subseteq P(A)$ .
- 2. (15 points) Advanced compilers could re-arrange machine instructions so as to optimize performance and resource utilization. Consider a piece of assembly code listed as follows. An instruction can not be executed until all its operands are ready. For example, I2 **must be executed no earlier** than I1 is. The situation can be expressed as I1 $\rightarrow$ I2. Let R =  $\{(I_a,I_b) | I_a \rightarrow I_b\}$  be a binary relation on the set of the five instructions.

```
11: ADD R3←R1,R2  ; add R1 to R2 and put the result in R3
12: SUB R4←R3,1  ; subtract 1 from R3 and put the result in R4
13: MOV [100],R4  ; put R4's content into memory location 100
14: MUL R1←R4,5  ; multiply R4 by 5 and then put the result in R1
15: MOV [200],R1  ; put the content of R1 into memory location 200
```

- (a) List all items in R.
- (b) Is R a partial order relation? Explain why or why not.
- 3. (10 points) An artist is coloring stained glass. Any two adjacent shapes on the glass must have different colors. What is the minimal number of colors the artist needs to paint the glass shown below?

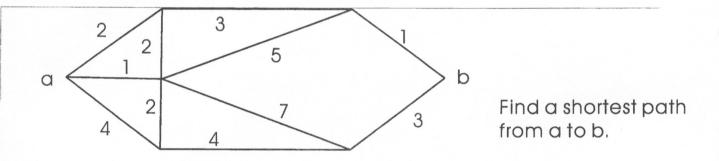


4. (15 points) Find the number of permutations of the six letters x,y,x,z,y,z so that no x appears in the first two elements, no y appears as the forth element, and no z appears in the last two elements.

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- 5. (10 points) Is it true that a group with p elements (where p is a prime number) must be cyclic? Why or why not?
- 6. (10 points) Prove that if there is a vertex of degree k in a tree, there must be k vertices of degree 1 in that tree.
- 7. (15 points) Please write an algorithm for finding a shortest path from a vertex to another vertex. Use the following figure to explain your algorithm. Vertex a is starting vertex and vertex b is the final vertex.



8. (15 points) Consider only positive integer written in decimal notation. Define a function f as follows: f moves the most significant digit of an integer to the least significant place. For instance, f(1234) = 2341, f(564) = 645, f(10032) = 321, etc. Find the least integer x such that  $f(x) = \frac{3x}{2}$ .